



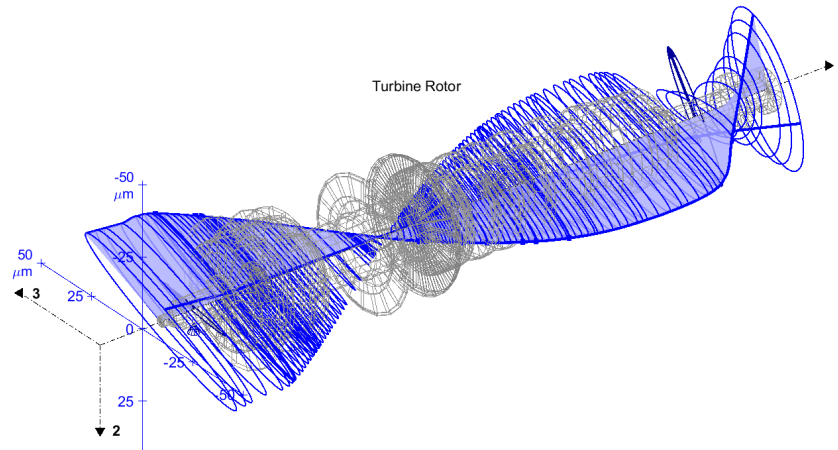
# 22<sup>nd</sup> Swiss CADFEM ANSYS Simulation Conference 2017

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## Coupled Rotor-Bearing-Casing Analysis

Gekoppelte Rotor-Gleitlager-Gehäuse Berechnung

Using State Space Matrices from ANSYS in **MADYN 2000**



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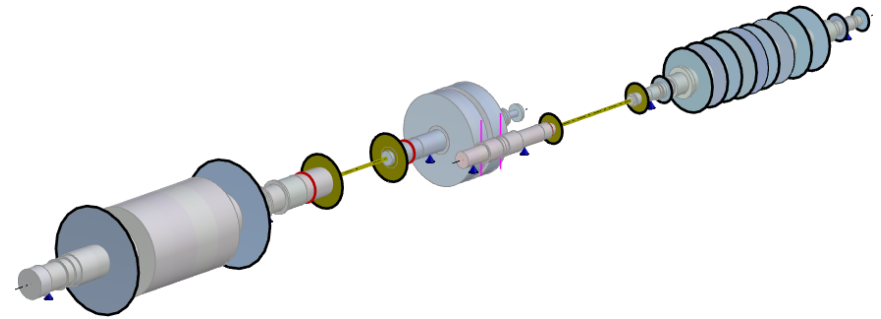


# Contents

- What is rotordynamics?
- Support modelling with spring & mass
- Support modelling with transfer functions
- Support modelling with state space matrices from ANSYS

# What is Rotordynamics?

- Rotordynamics is the analysis of rotating machines for their vibration behaviour.
- Systems can consist of rotors, bearings, supports & gears.
- Fluid film (or active magnetic) bearings are the main source of damping for the lateral vibrations. They can also destabilize.
- It is possible to carry out rotordynamic analyses with general FE or multibody dynamics programs. However, specialised rotordynamics software such as **MADYN 2000** has proven to be most efficient for daily work.





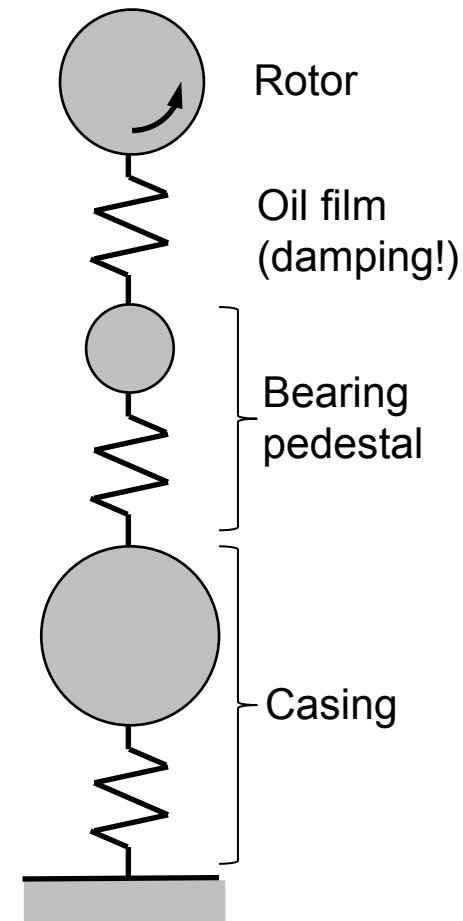
# What is Rotordynamics? Analysis with MADYN 2000

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- Concentration on modelling with Timoshenko beams, which are well suited for shafts.
- Speed and / or frequency dependent bearings (→ fluid film, active magnetic, rolling elements) are integrated.
- Consideration of gyroscopic forces.
- Efficient modelling, analysis and post-processing.
- The dynamic properties of complex support structures such as casings or foundations cannot be determined directly in MADYN 2000. But they can be imported into the system.

# What is Rotordynamics? Bearings and Support Structure

- The bearings enable the rotation of the shaft and can provide damping of the lateral vibrations (e.g. through movement of the shaft in the oil film).
- The support structure (→ pedestal, casing, base frame, foundation) also contributes to the flexibility of the system. The support structure must be considered in the model unless it is much stiffer than the bearing.

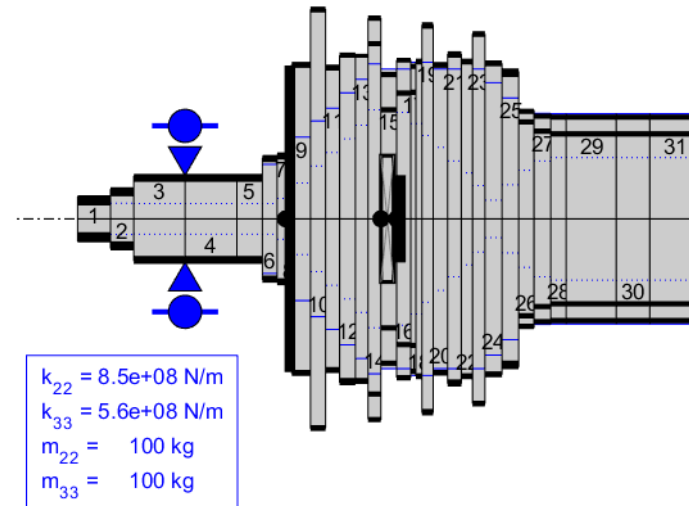
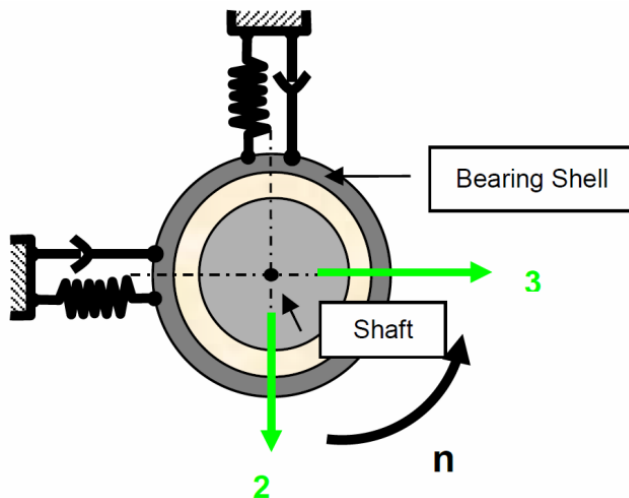




# Support Modelling with Spring & Mass

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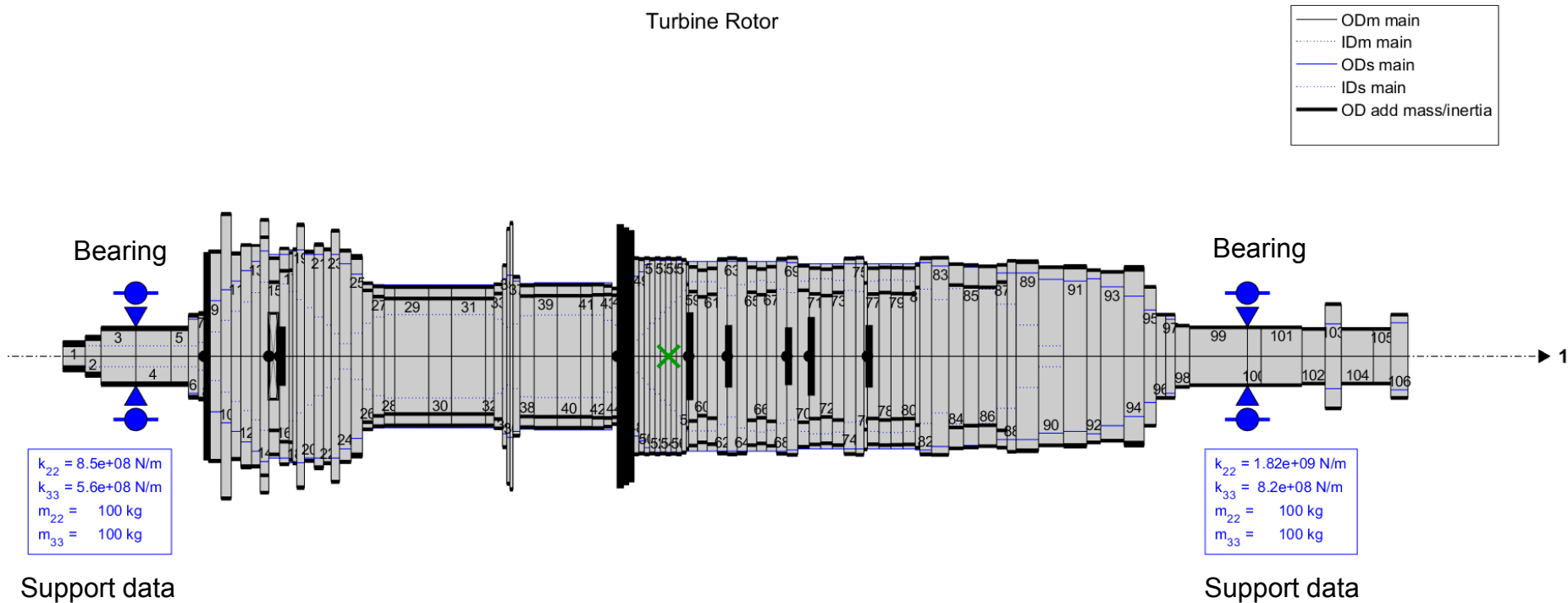
- The spring & mass support is a traditional and still widely used approach to consider pedestal, casing etc.
- Only 1 degree of freedom per bearing / direction.
- No coupling effects between the bearings.





# Support Modelling with Spring & Mass Rotordynamic Model – Turbine Shaft

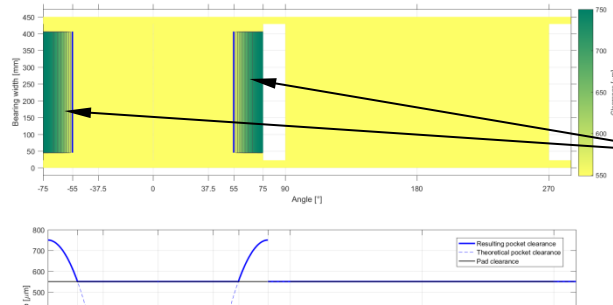
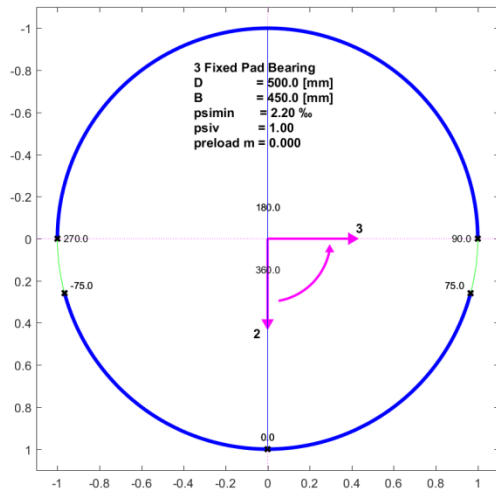
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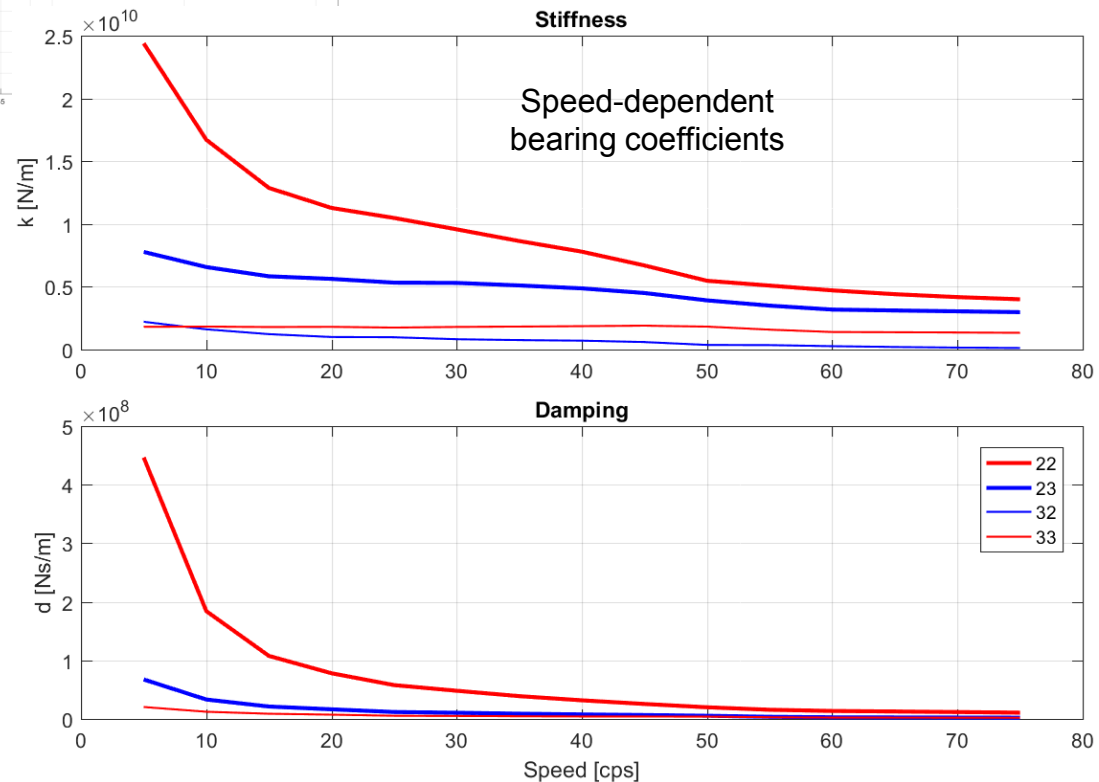
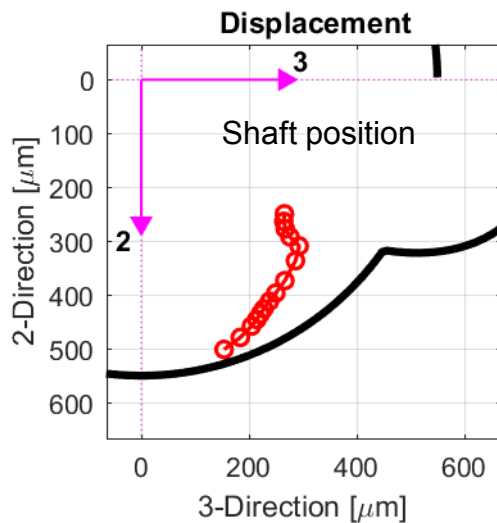
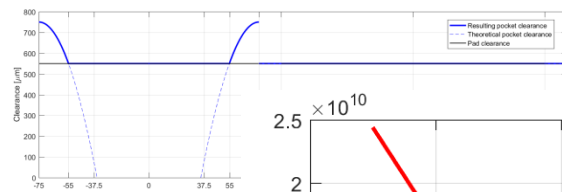


# Support Modelling with Spring & Mass Rotordynamic Model – Fluid Film Bearing

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Hydrodynamic pockets (oil wedges)

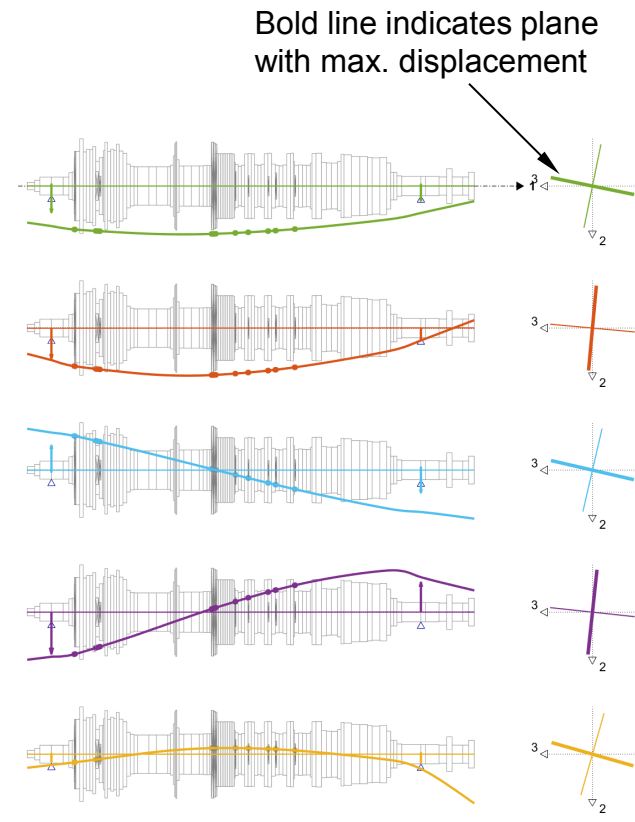
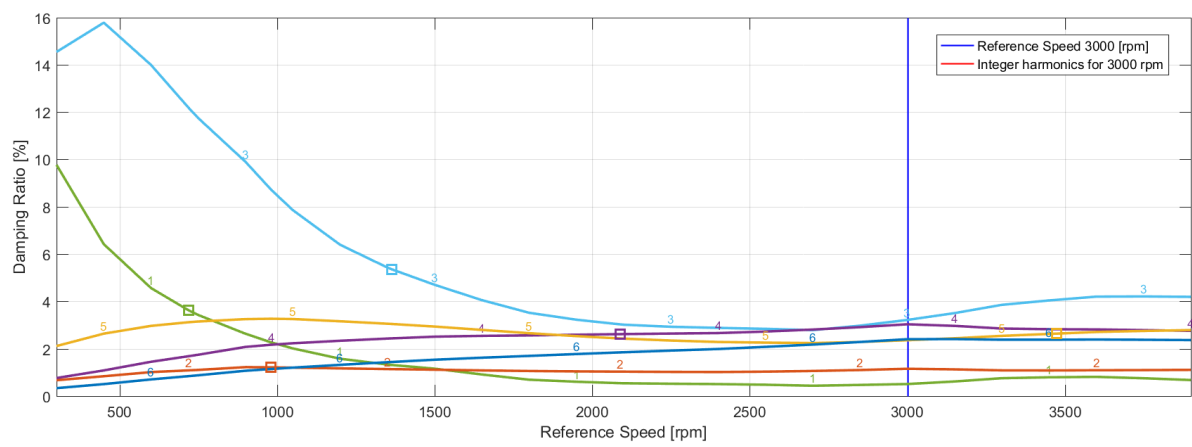
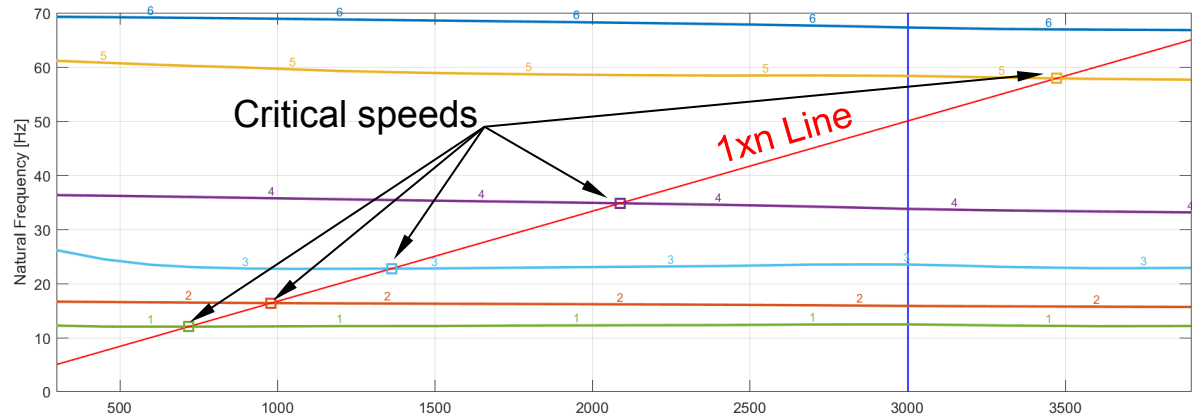






# Support Modelling with Spring & Mass Campbell Diagram and Critical Modes

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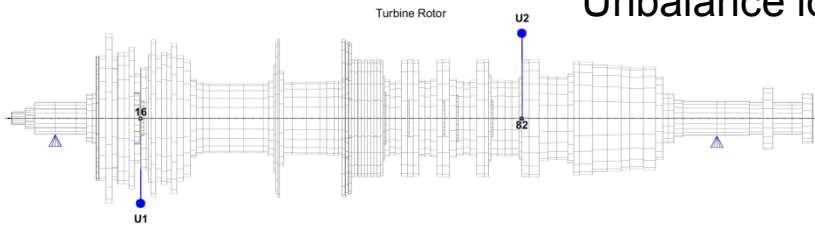


# Support Modelling with Spring & Mass

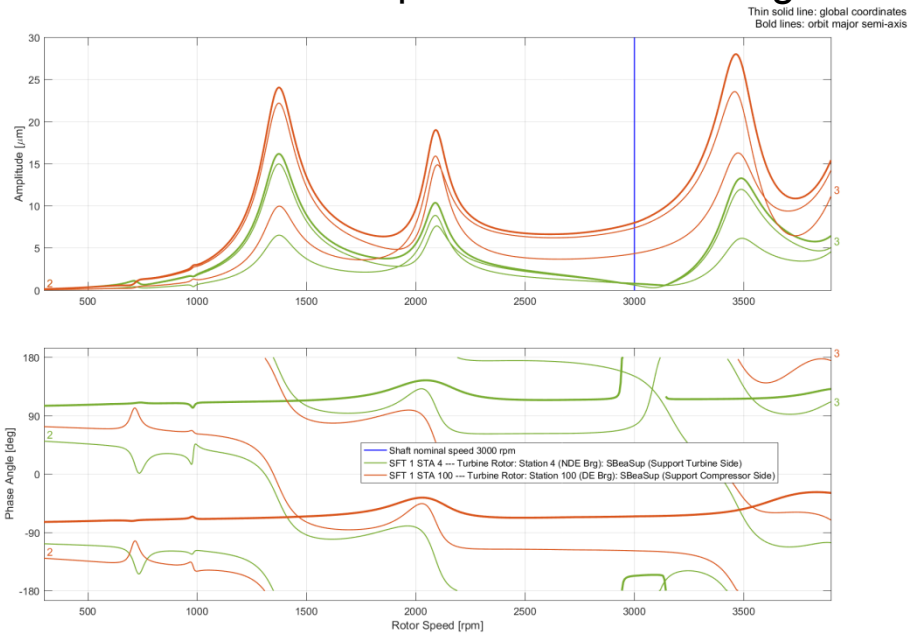
## Unbalance Response

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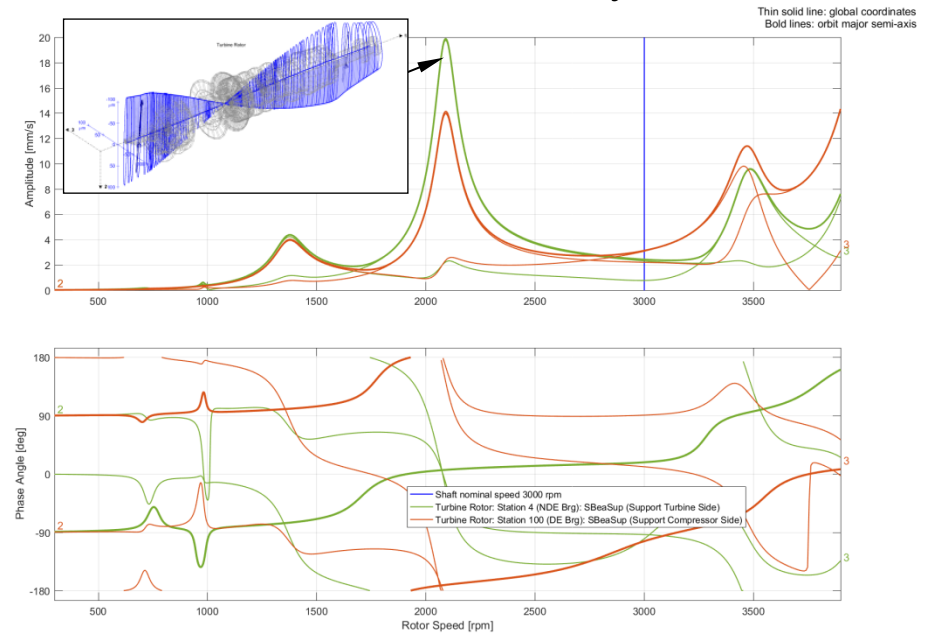
### Unbalance load case



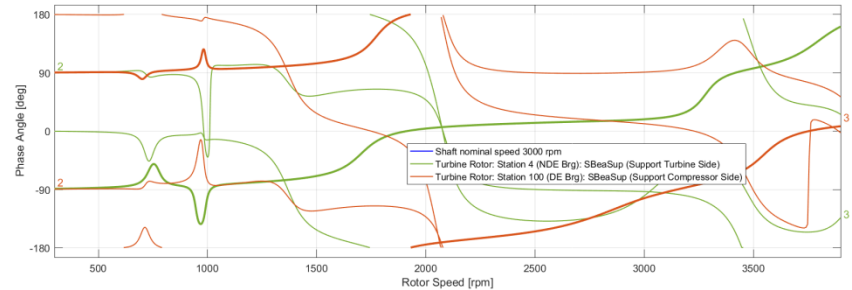
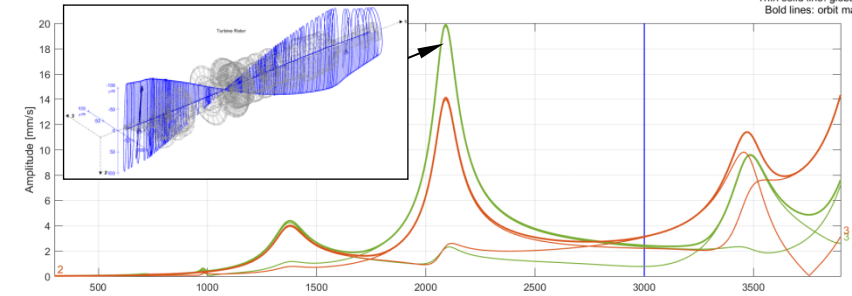
### Relative shaft displacement at bearings



### Pedestal velocity



Thin solid line: global coordinates  
Bold lines: orbit major semi-axis

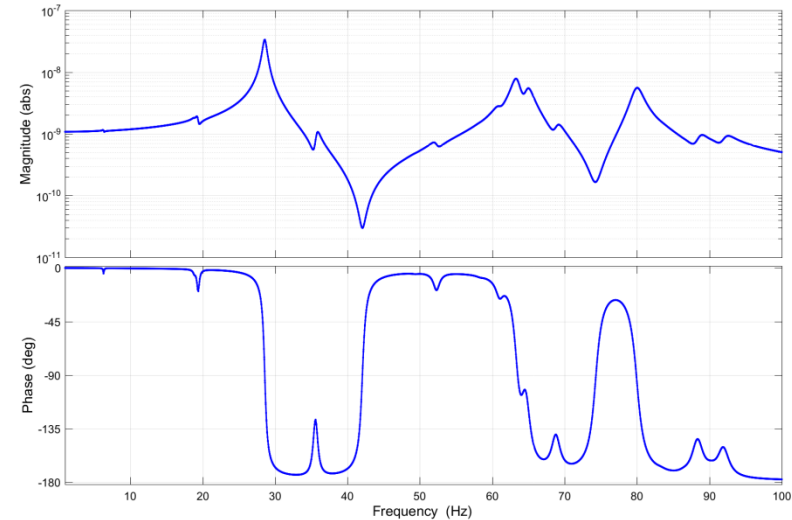




# Support Modelling with Transfer Functions

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- Transfer functions describe the dynamic (i.e. frequency-dep.) flexibility of the support structure.
- They can be calculated with an FE program (→ harmonic response analysis) or measured.
- Creating and importing transfer functions can be time-consuming for systems with many bearings.
- Fitting polynomials to the imported transfer functions is required for eigenvalue analyses, but is sometimes difficult.



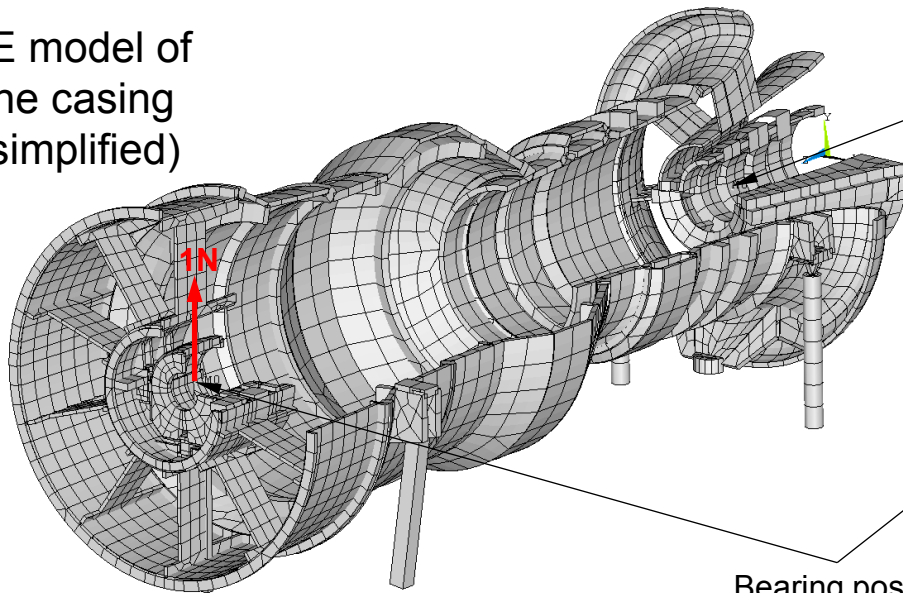


# Support Modelling with Transfer Functions

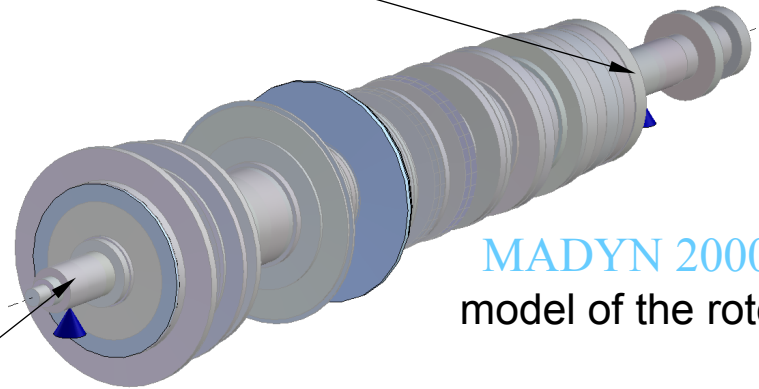
## Calculating the TF in ANSYS

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FE model of the casing (simplified)



Bearing position



MADYN 2000  
model of the rotor

Bearing position

\*\*\*\*\* ANSYS POST26 VARIABLE LISTING \*\*\*\*\*

List of the response for 1N vertical harmonic excitation and 1% damping ratio.  
(Transfer functions are imported into MADYN 2000 as text files.)

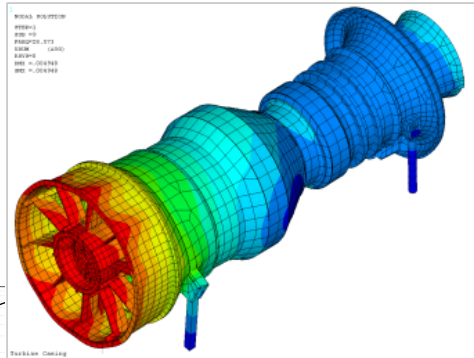
| FREQ    | NSOL UY<br>Exhaust<br>AMPLITUDE | PHASE         |
|---------|---------------------------------|---------------|
| 0.10000 | 0.107840E-08                    | -0.323132E-02 |
| 0.20000 | 0.107843E-08                    | -0.646297E-02 |
| 0.30000 | 0.107848E-08                    | -0.969526E-02 |
| 0.40000 | 0.107855E-08                    | -0.129285E-01 |
| 0.50000 | 0.107864E-08                    | -0.161631E-01 |
| 0.60000 | 0.107875E-08                    | -0.193993E-01 |
| 0.70000 | 0.107888E-08                    | -0.226375E-01 |



# Support Modelling with Transfer Functions

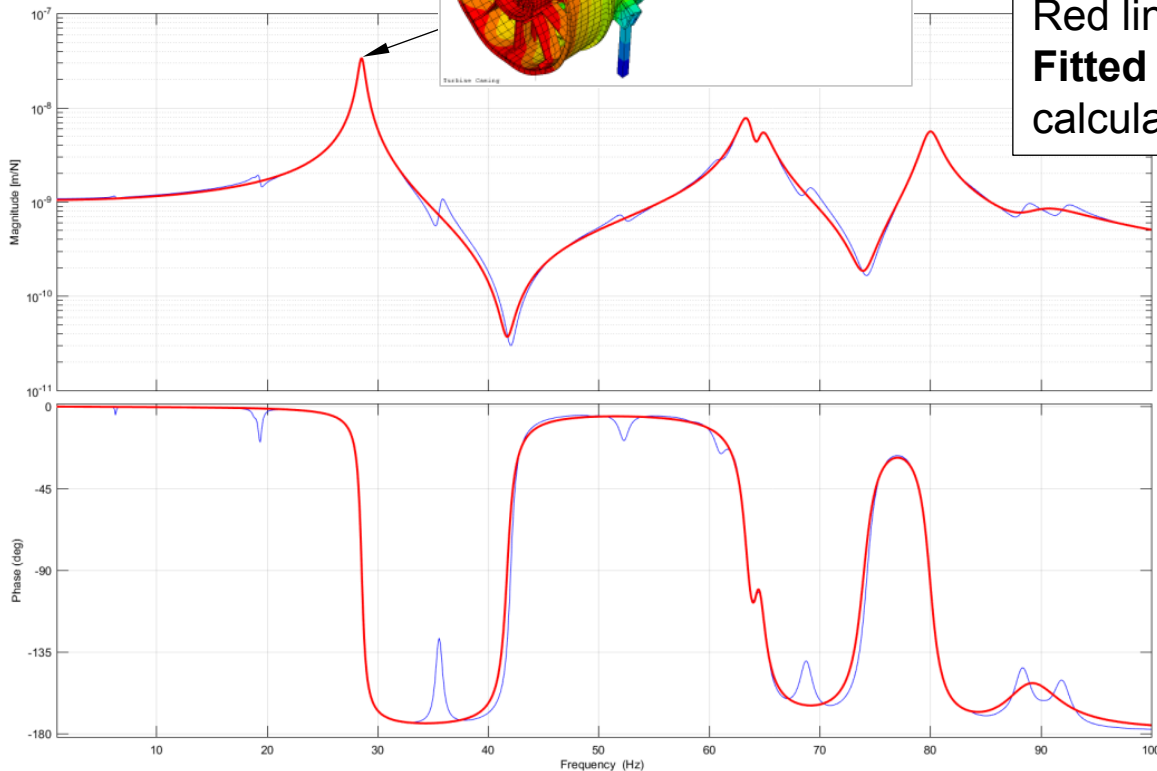
## Importing the Transfer Functions

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Blue line:  
Imported source data → used for harmonic analysis (e.g. unbalance response)

Red line:  
**Fitted polynomial** → required for the calculation of the damped eigenvalues





# Support Modelling with State Space Matrices from ANSYS

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- In **MADYN 2000** the support structure can be considered in the form of state space matrices. This allows damped eigenvalue analyses of the rotor without fitting polynomials.
- The state space matrices can be created in ANSYS from the results of the modal analysis in post-processing via the command **SPMWRITE**.
- The interface nodes (i.e. the nodes at the centres of the bearings) and the directions have to be defined. The state space matrices are written to **Jobname.spm**.
- Modal damping for the modes considered in the state space matrices has to be introduced during import to **MADYN 2000**.



# Support Modelling with State Space

## Basics of State Space Matrices

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- Any linear dynamic system can be represented in State Space form:  
$$\dot{z} = A z + B u$$
$$y = C z + D z$$
- $u$  inputs to a system,  $y$  outputs,  $z$  states,  
 $A, B, C, D$  system, control or input, observer and direct transition matrices.
- In [MADYN 2000](#) State Space representation is used for various components such as magnetic bearings or fluid film tilting pad bearings and coupled dynamic supports.
- Bearings:  $u$  displacement and velocities,  $y$  forces.  
Supports:  $u$  forces,  $y$  displacement and velocities. The states  $z$  are the modal coordinates of considered modes,  $A$  contains natural frequencies,  $B$  and  $C$  components of eigenvectors,  $D$  is zero.



# Support Modelling with State Space

## The Import GUI in MADYN 2000

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The screenshot shows the MADYN 2000 interface with several overlapping windows. The main window displays system parameters for 'Turbine with DBS'. A 'DBS - DynBeaSup' dialog is open, showing a table of shaft stations and their associated bearings. A 'SSM - StateSpaceModel' dialog is also open, showing matrices A, B, and C, and a checkbox for 'Structural Damping [%]' which is checked and set to 1. Arrows point from the text 'Symmetric' to the Matrix A field and from 'Specify damping' to the Structural Damping checkbox.

| Shaft (Turbine Rotor) | Station 4 (NDE Brg) | Station 100 (DE Brg) |
|-----------------------|---------------------|----------------------|
| 2                     | 3                   | 3                    |
| 2                     | 2                   | 2                    |
| 3                     | 3                   | 3                    |

Natural frequencies of the casing

| Fréquency [Hz] | Damping Ratio [%] |
|----------------|-------------------|
| 6.313          | 1.00              |
| 11.089         | 1.00              |
| 18.837         | 1.00              |
| 18.840         | 1.00              |
| 19.341         | 1.00              |
| 20.376         | 1.00              |
| 22.041         | 1.00              |
| 25.239         | 1.00              |
| 28.573         | 1.00              |
| 35.741         | 1.00              |
| 37.478         | 1.00              |
| 42.101         | 1.00              |
| 49.390         | 1.00              |
| 52.234         | 1.00              |
| 52.806         | 1.00              |
| 58.181         | 1.00              |
| 58.327         | 1.00              |
| 59.385         | 1.00              |
| 61.017         | 1.00              |
| 63.363         | 1.00              |
| 64.914         | 1.00              |
| 65.395         | 1.00              |
| 66.636         | 1.00              |
| 68.520         | 1.00              |
| 68.952         | 1.00              |
| 69.983         | 1.00              |
| 72.577         | 1.00              |
| 79.974         | 1.00              |
| 80.796         | 1.00              |
| 83.275         | 1.00              |
| 83.434         | 1.00              |
| 86.500         | 1.00              |
| 87.533         | 1.00              |
| 88.591         | 1.00              |
| 88.705         | 1.00              |
| 90.248         | 1.00              |
| 90.429         | 1.00              |
| 90.940         | 1.00              |
| 92.130         | 1.00              |
| 93.097         | 1.00              |
| 94.354         | 1.00              |
| 97.487         | 1.00              |





# Support Modelling with State Space

## The Transfer Functions

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Transfer functions from the state space system.



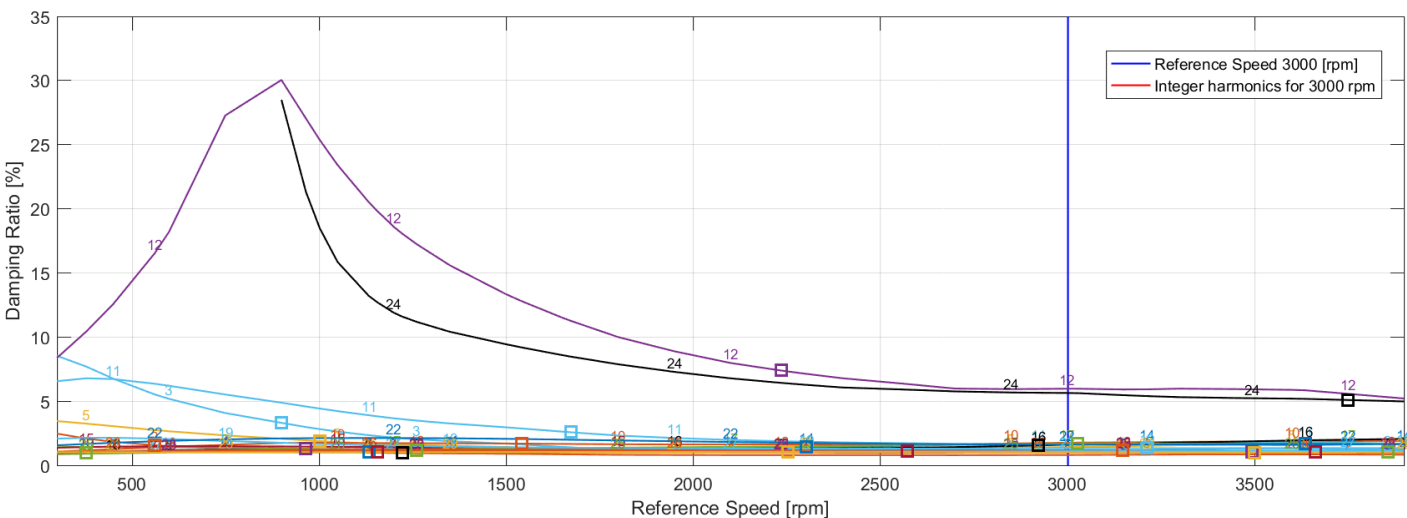
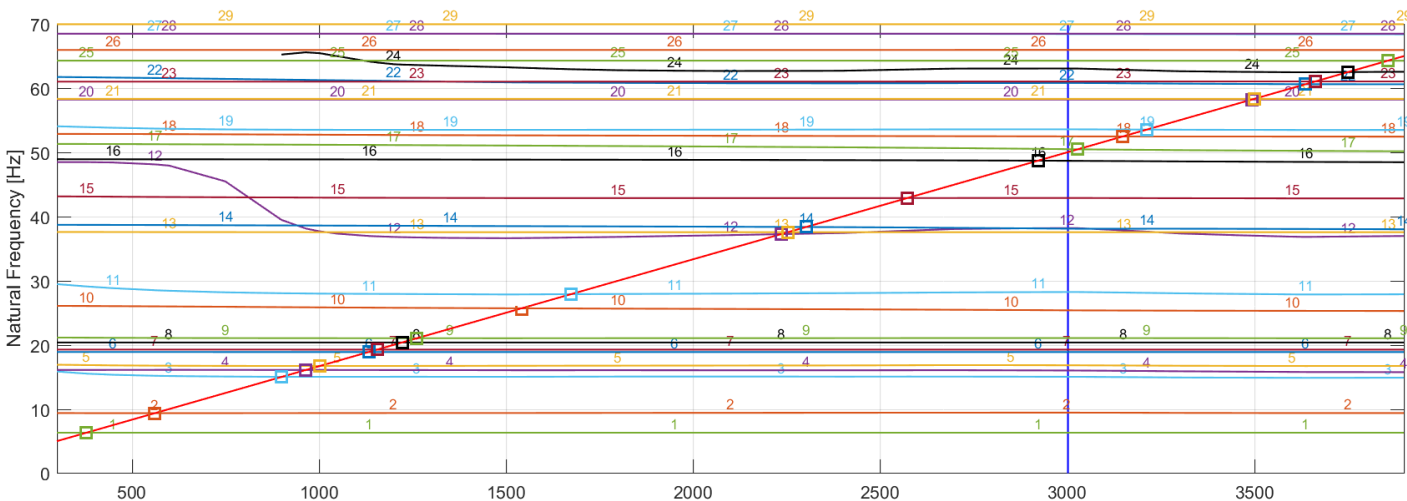
Low values indicate little coupling between the vertical and the horizontal direction



# Support Modelling with State Space Campbell Diagram

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Many additional modes are caused by the casing.





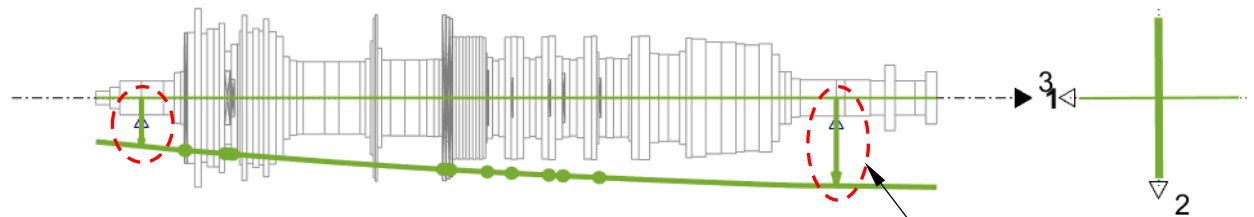
# Support Modelling with State Space

## Examples of Critical Modes

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### Pure casing mode

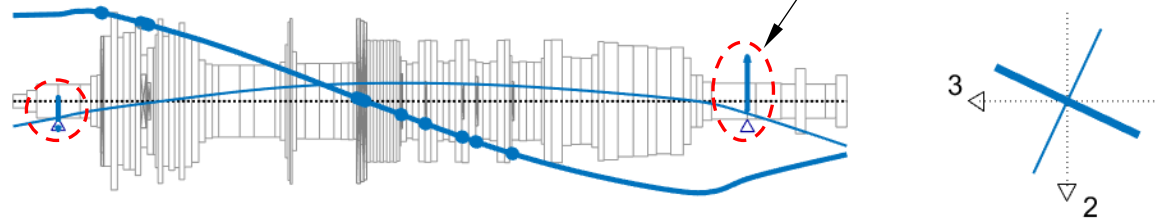
Mode: 1  
Frequency: 6.31 Hz  
378.6 cpm  
Damping: 1.0 %  
Whirling direction: +0.00



Arrow = Casing displacement

### Coupled rotor-casing mode

Mode: 14  
Frequency: 38.20 Hz  
2292.3 cpm  
Damping: 6.0 %  
Whirling direction: +0.07

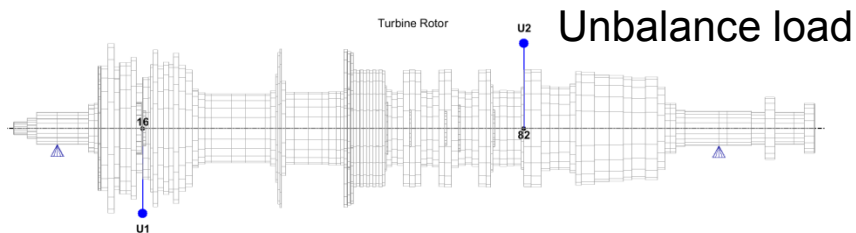




# Support Modelling with State Space

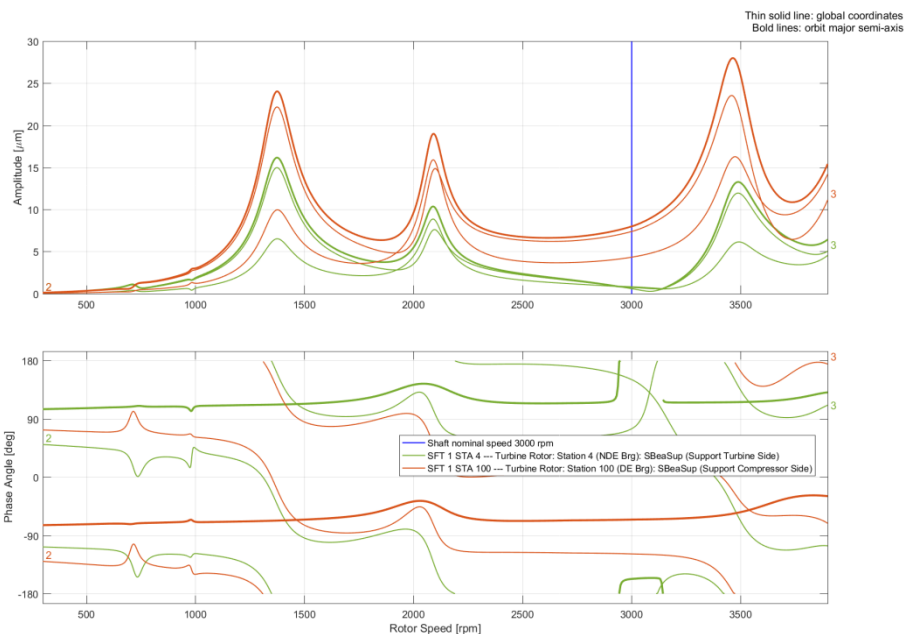
## Unbalance Response

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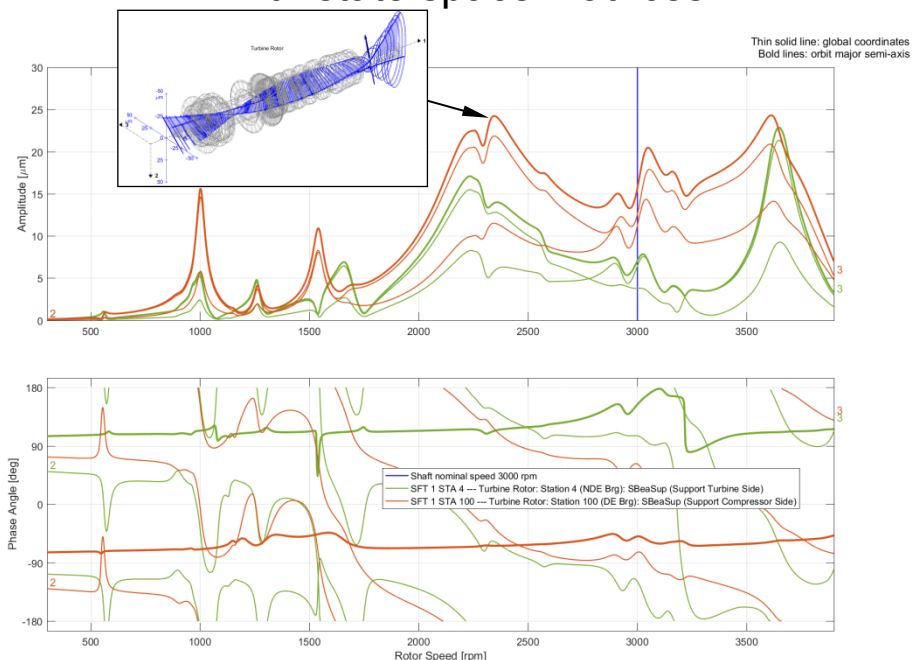


Comparison of the relative shaft displacement at the bearings.

With spring & mass



With state space matrices





# Conclusion

- A specialised software such as [MADYN 2000](#) is an efficient tool for rotordynamic analyses.
- ANSYS as a general FE program is well suited to analyse complex support structures of turbomachines.
- State space matrices, which exactly describe the dynamic properties of the support structure, can be created with ANSYS and then imported into [MADYN 2000](#).
- The presented method enables a rotordynamic model, which is both accurate and lean. Thus, it combines the best of two worlds.